

# MethaneSAT L4 CORE: Conserved and Optimized Retrieval of Emissions



**The MethaneSAT and MethaneAIR Science and Engineering Teams**

**Presented by Jacob Bushey**

**Wofsy Group, Harvard University**

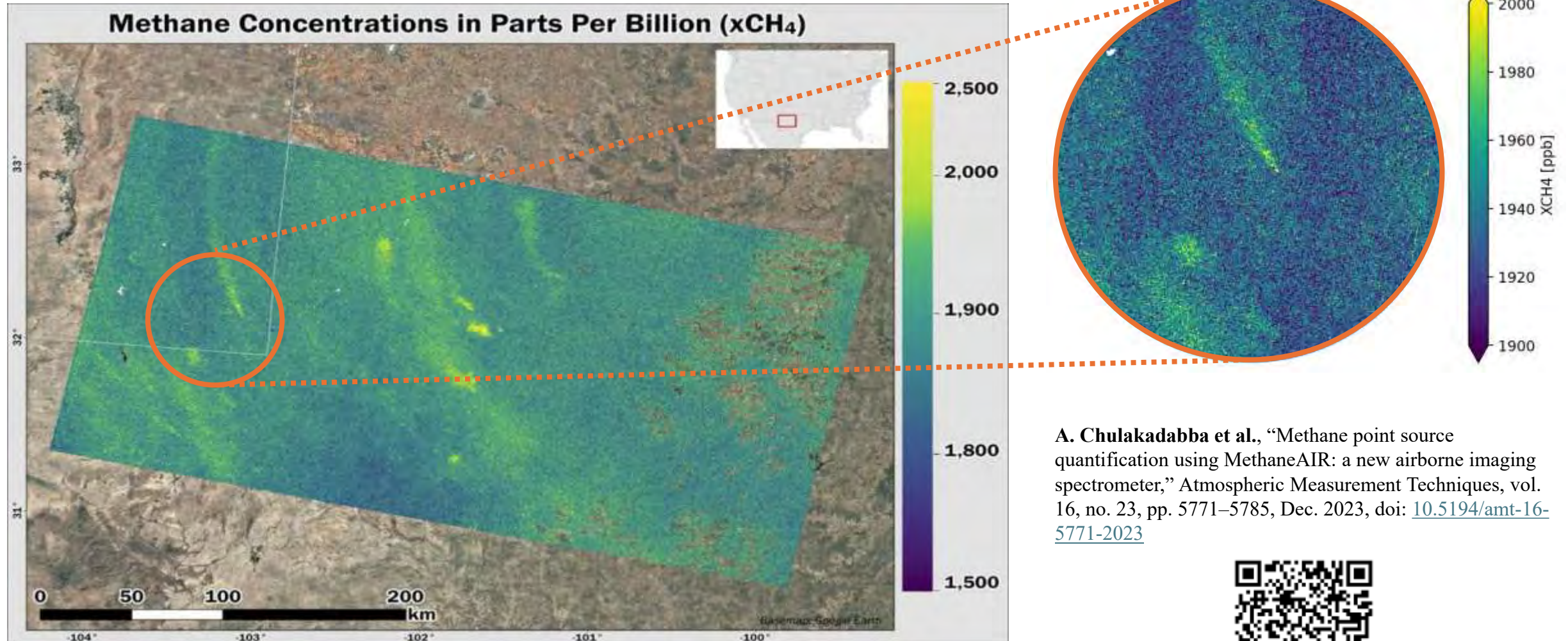
**[jbushey@g.harvard.edu](mailto:jbushey@g.harvard.edu)**



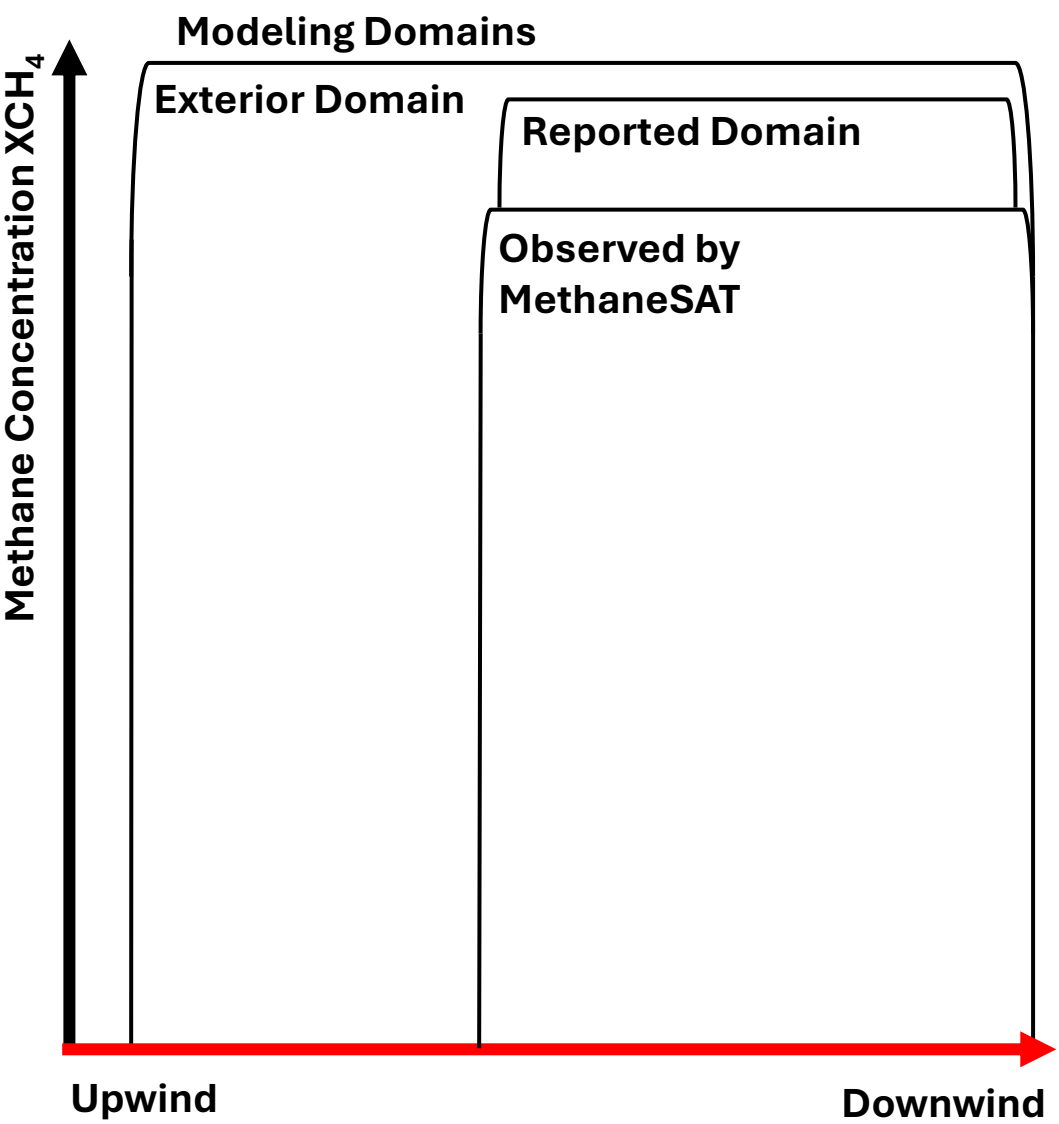
**Harvard** John A. Paulson  
**School of Engineering**  
and Applied Sciences



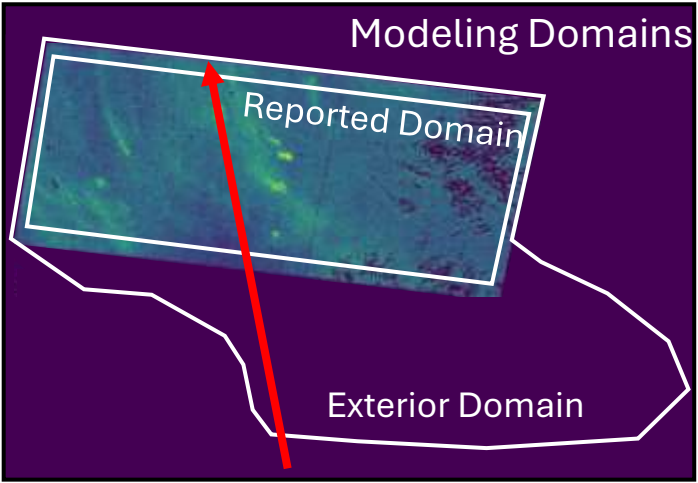
# The instrument combines high sensitivity and spatial resolution to observe both point and area sources



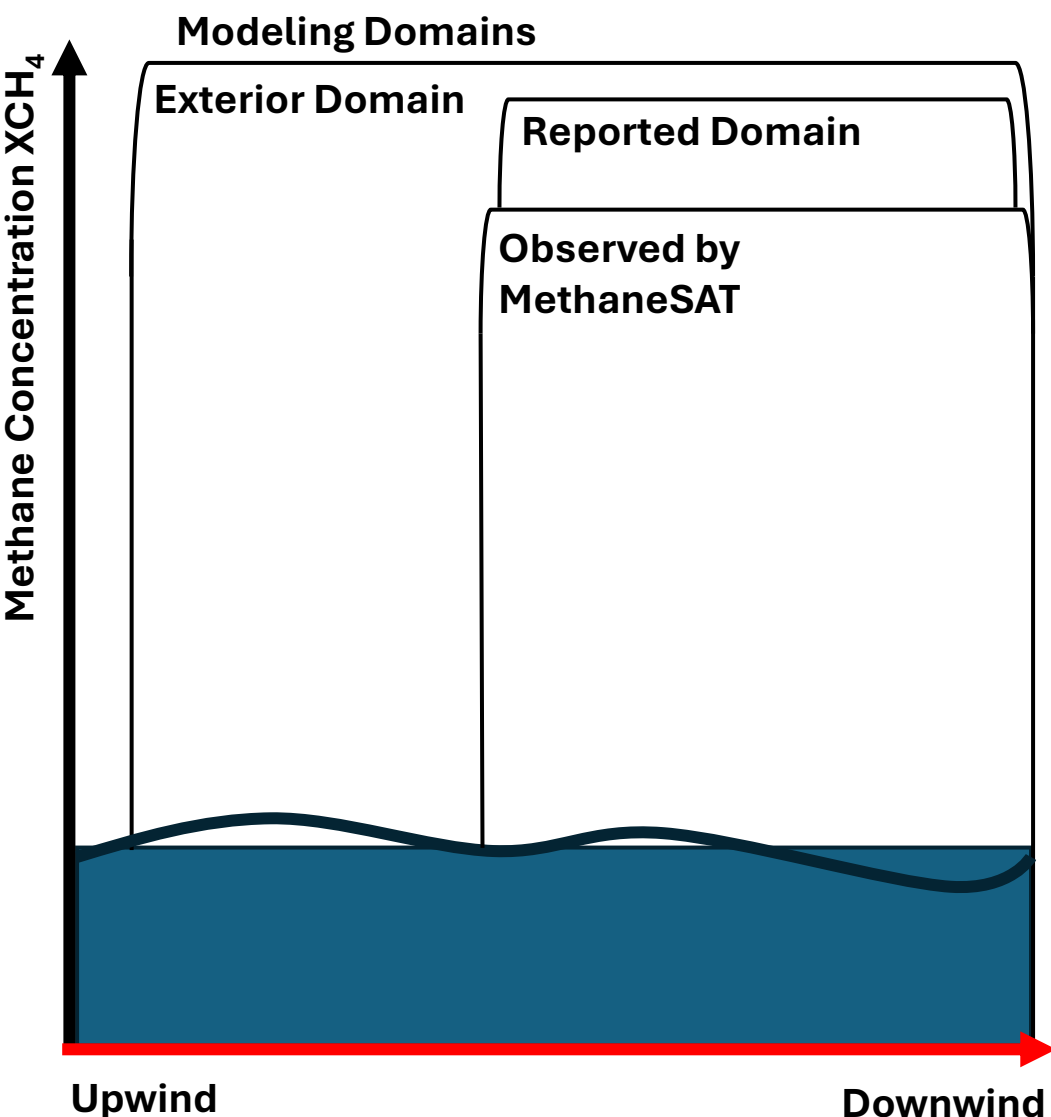
# MethaneSAT observations reveal the spectrum of scales of variability of methane concentrations and emissions



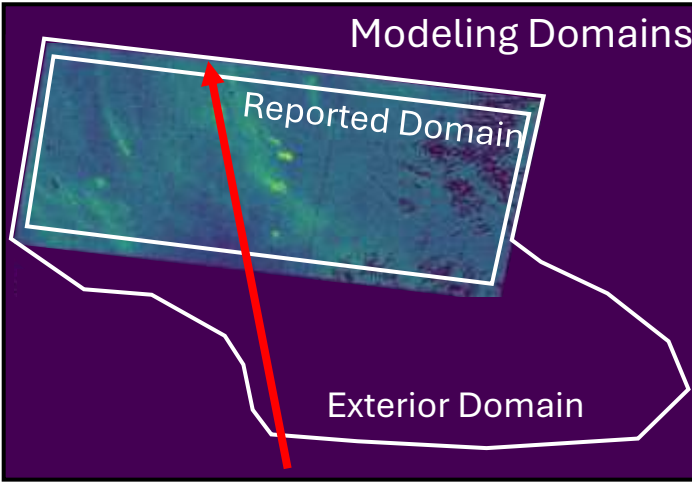
Examining variability along a transect



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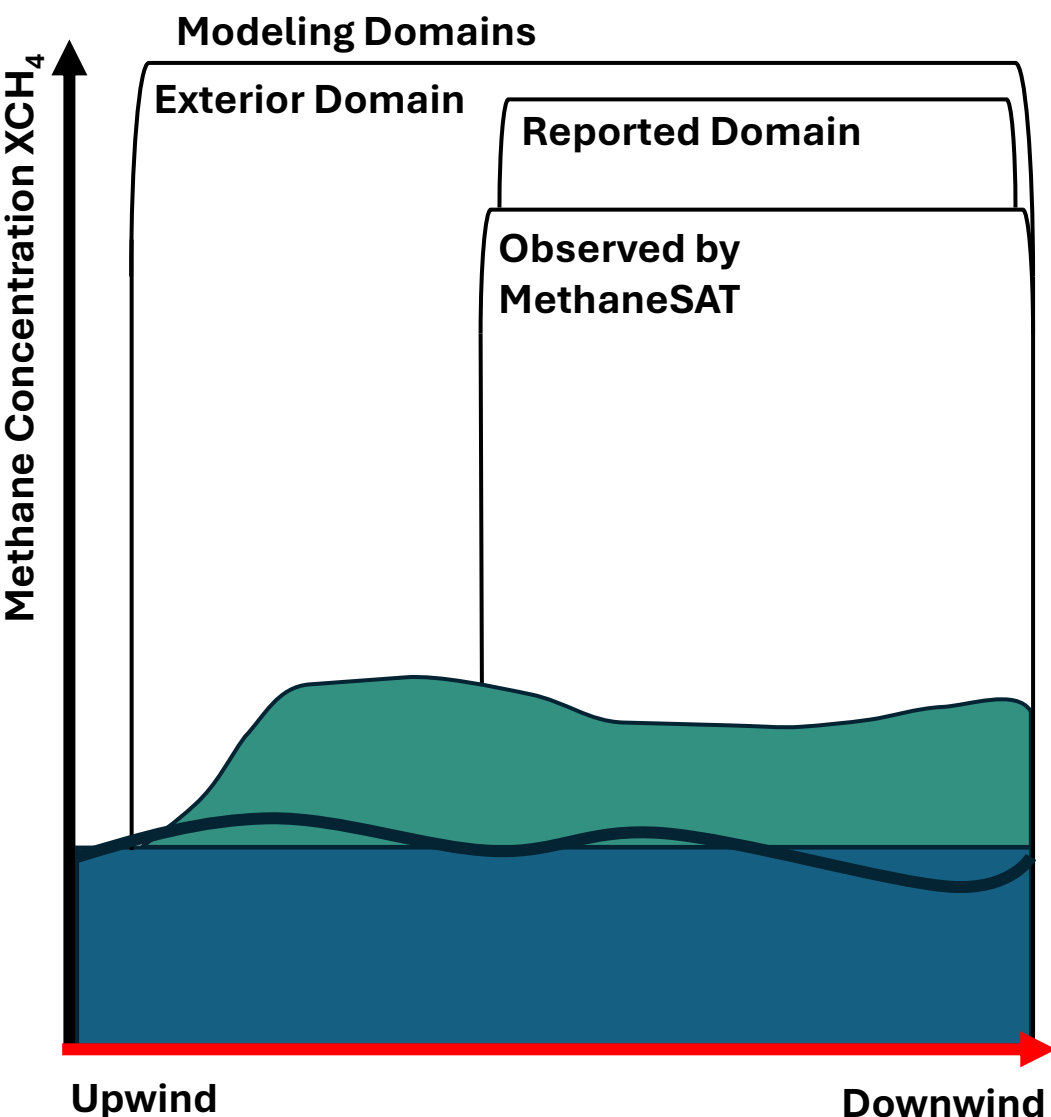


Examining variability along a transect

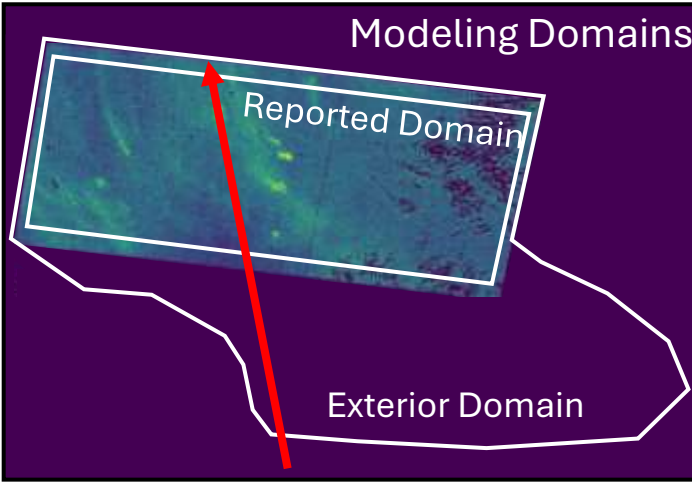


**Regional Background** A constant value for the entire scene: the lowest concentrations above measurement noise plus variations due to the topographical column effect.

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Examining variability along a transect



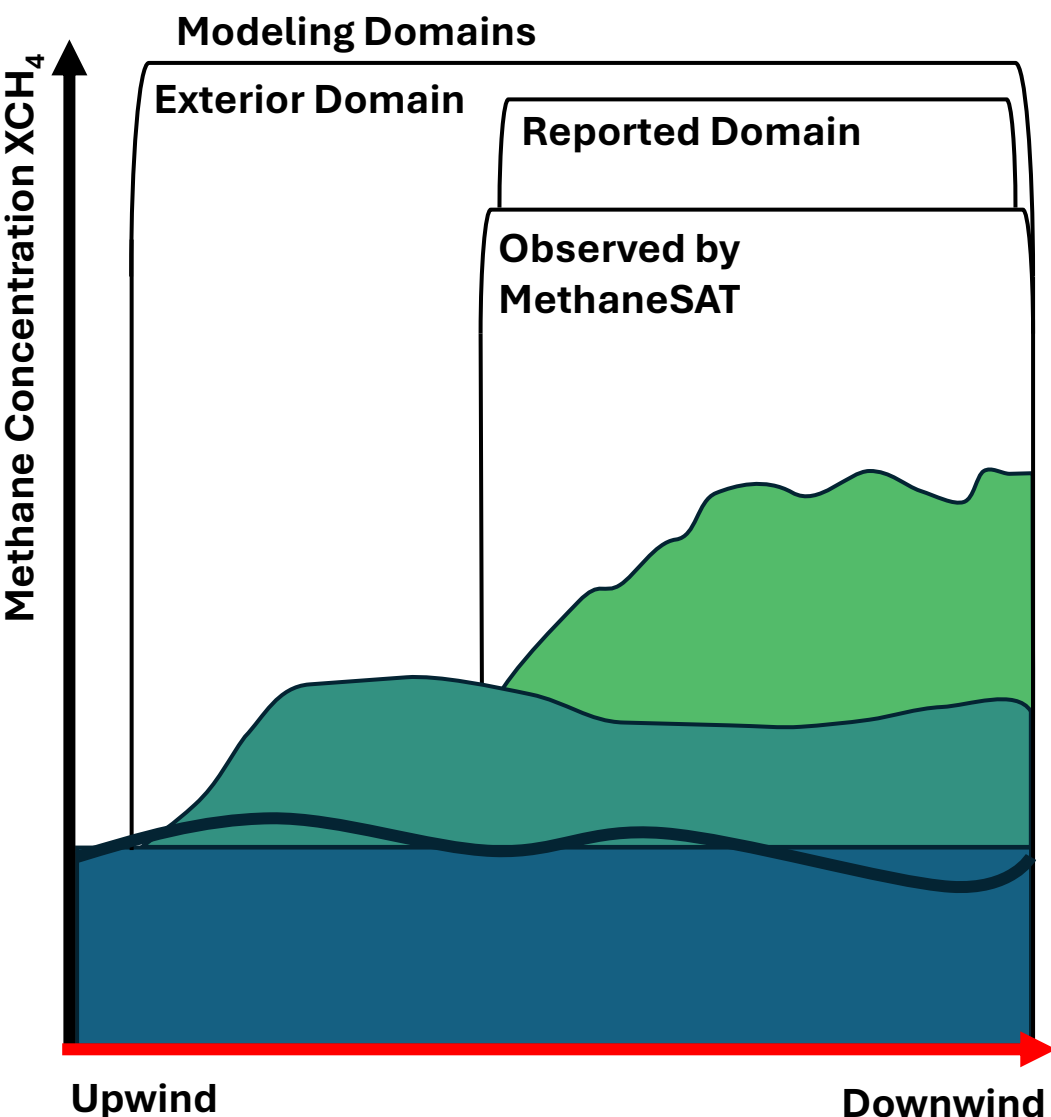
Boundary Inflow

Higher frequencies near the inflowing edge of the reported domain.  
Lower frequencies in the interior of the local domain.  
Modeled with “pseudo-emissions” in the exterior domain.

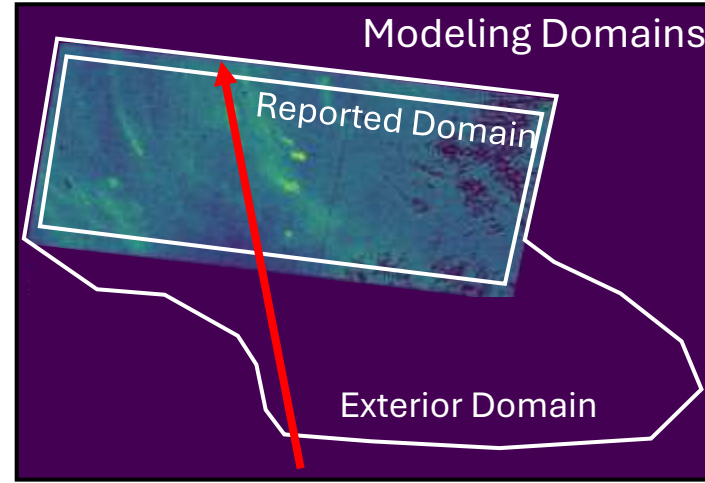
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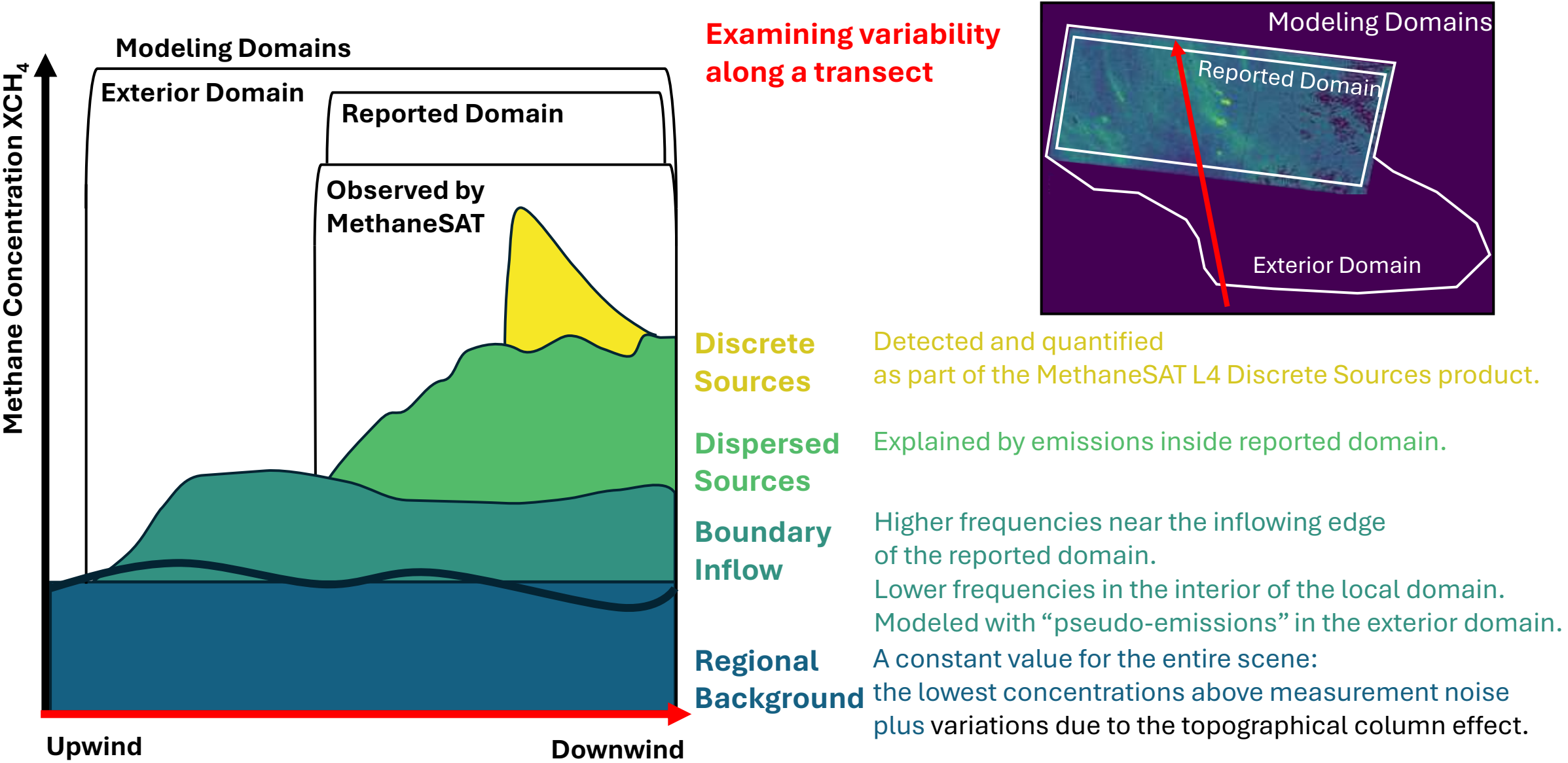
Examining variability along a transect



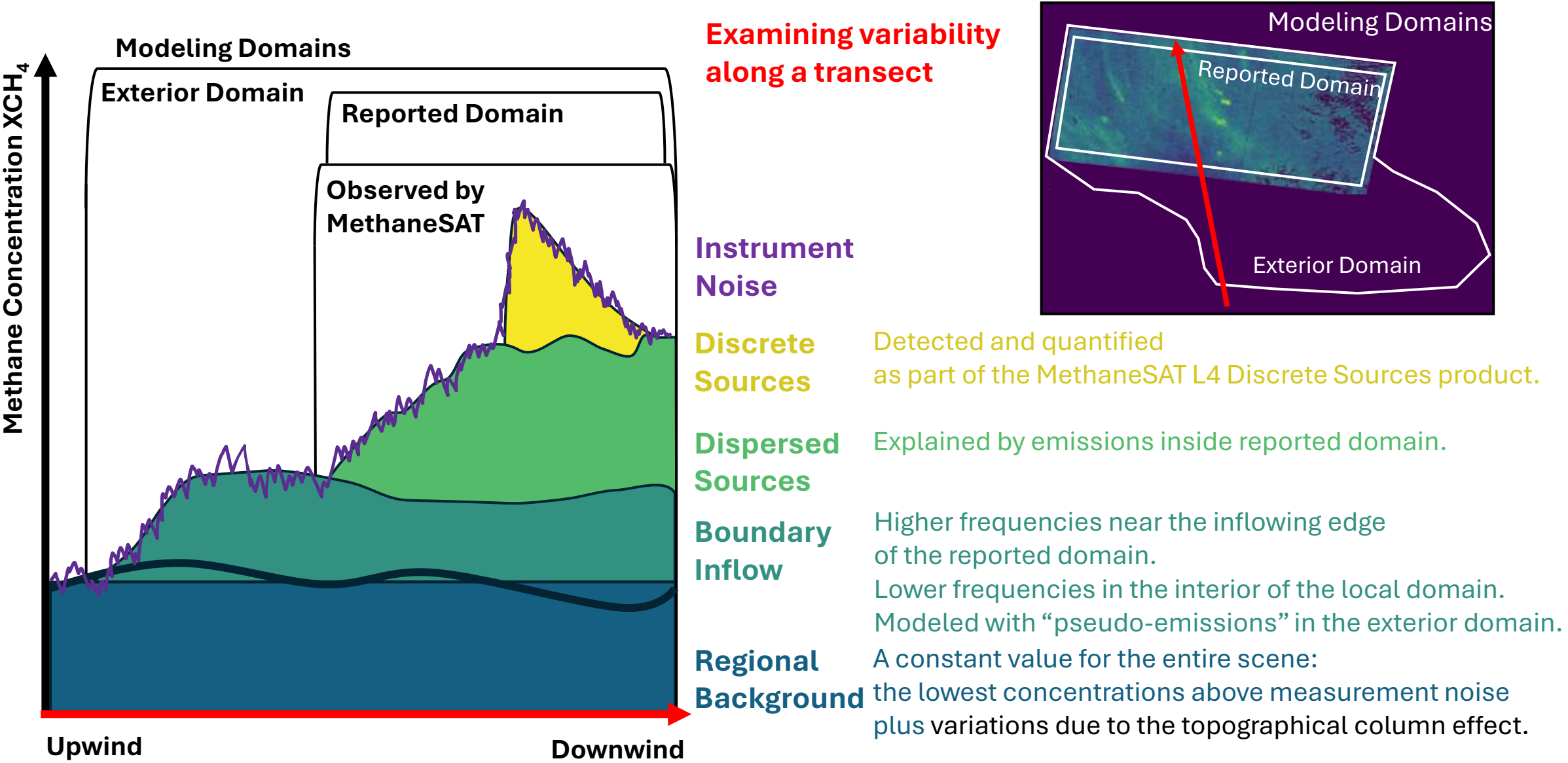
- Dispersed Sources** Explained by emissions inside reported domain.
- Boundary Inflow** Higher frequencies near the inflowing edge of the reported domain.  
Lower frequencies in the interior of the local domain.  
Modeled with “pseudo-emissions” in the exterior domain.
- Regional Background** A constant value for the entire scene:  
the lowest concentrations above measurement noise plus variations due to the topographical column effect.



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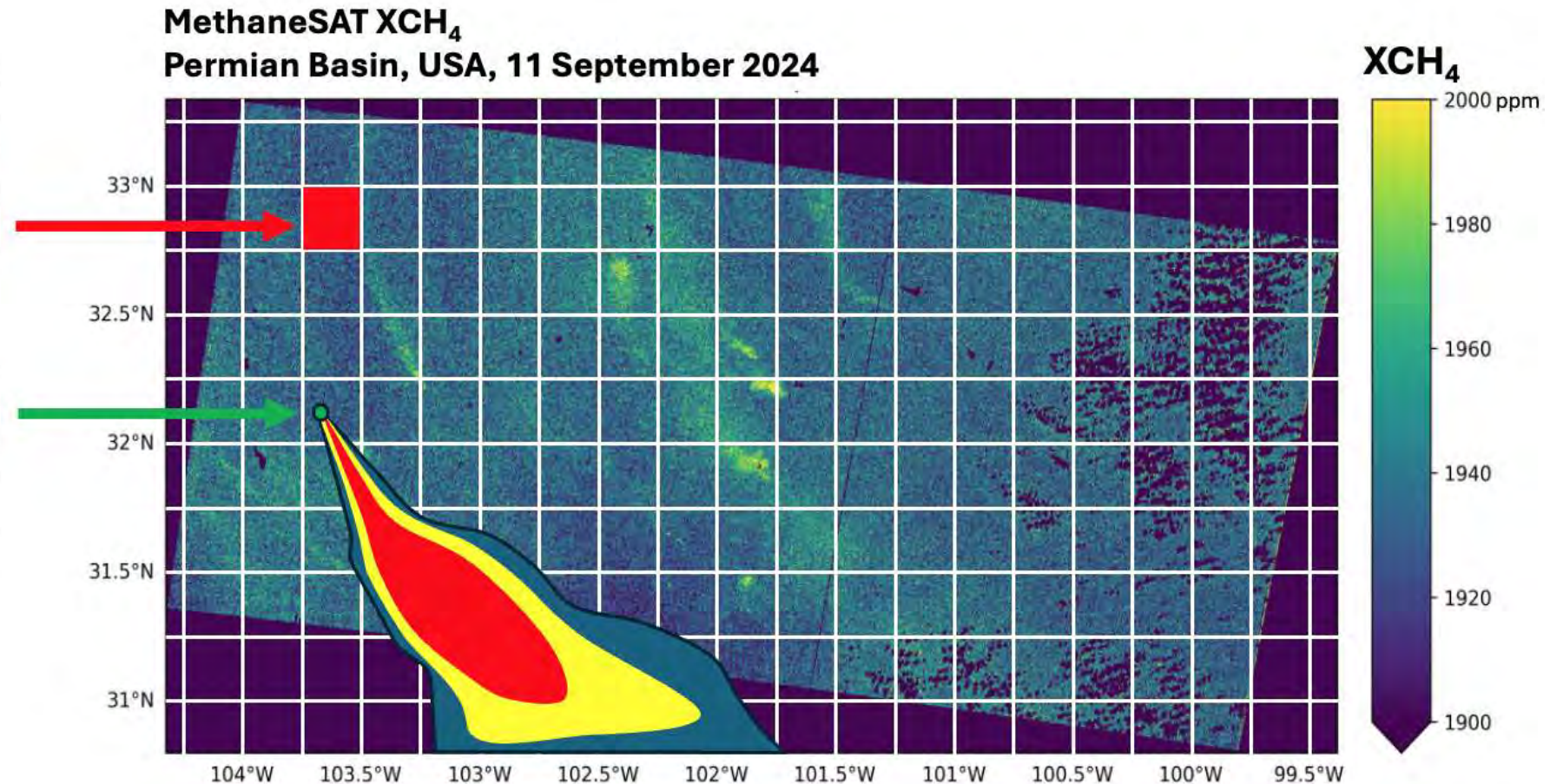




# We use STILT, driven by operational meteorology, to model transport backwards in time

A 0.25° Eulerian grid cannot fully utilize the spatial richness of MethaneSAT data.

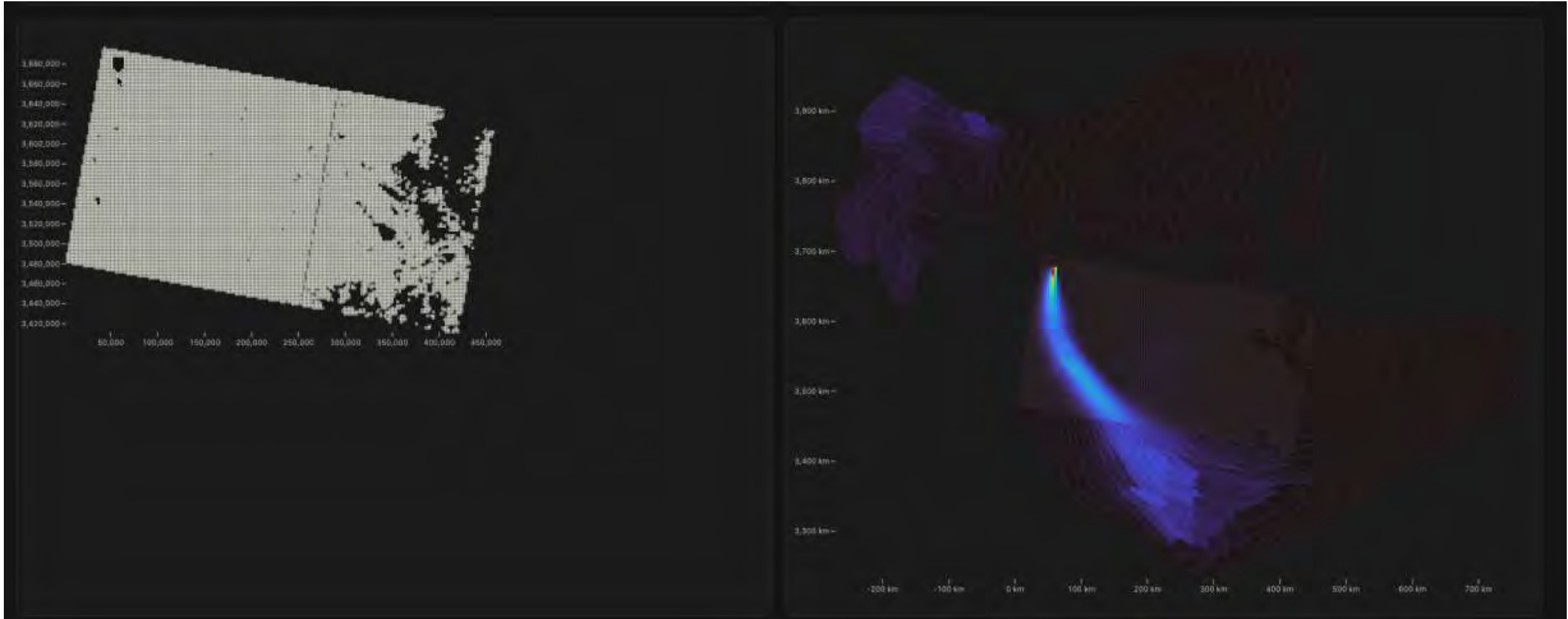
The Lagrangian nature of the STILT model resolves sub-grid scale variability.



1. Lin et al., 2003

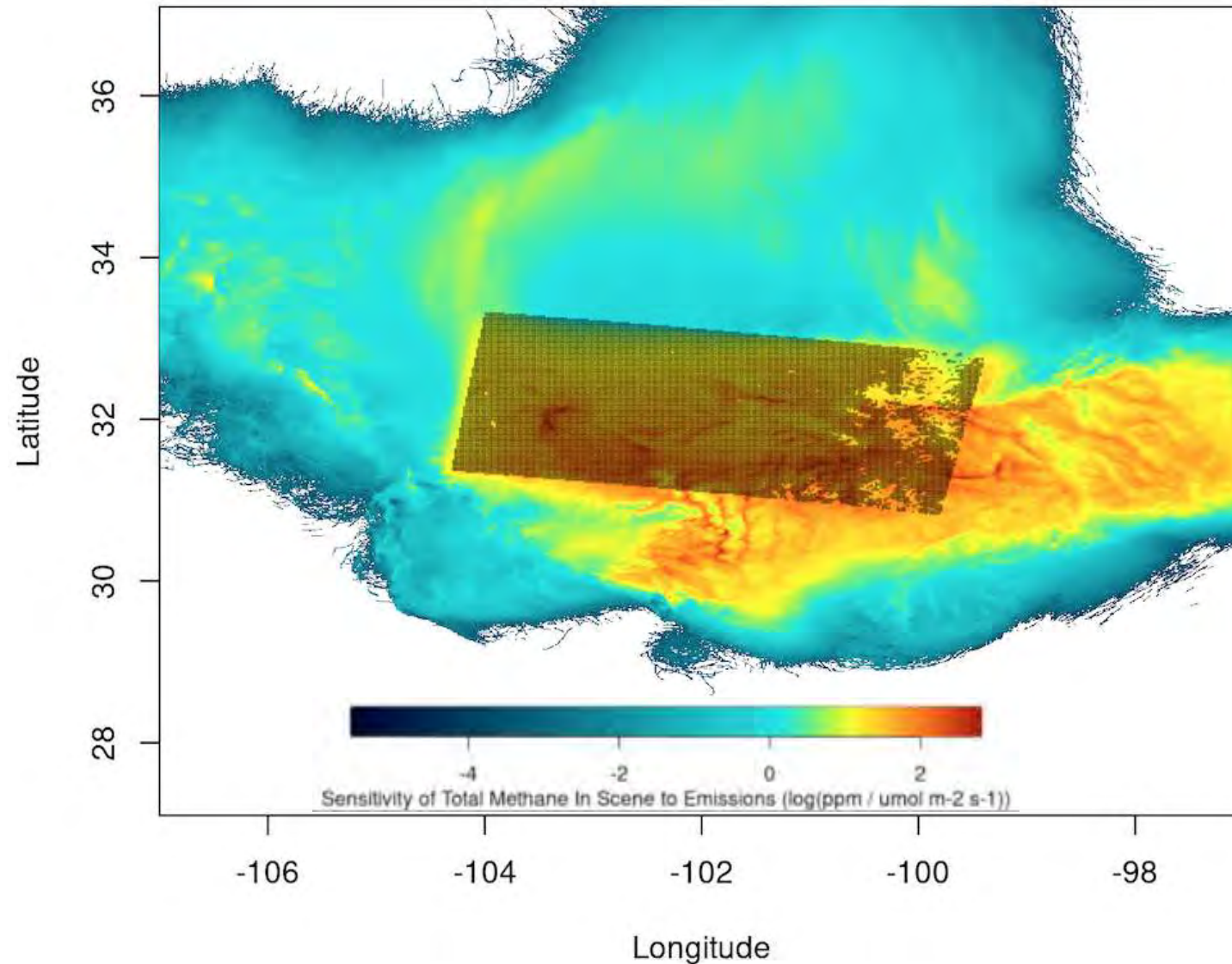
2. Fasoli et al., 2018

**We model a footprint for each observation,  
allowing us to determine the region of influence for emissions**





**The footprints of influence define the source-receptor relationships which will become our Jacobian matrix**



# The observations can be decomposed into constituent parts

$$\mathbf{z} = \mathbf{H}\mathbf{s} + \mathbf{b} + \boldsymbol{\varepsilon}_0$$

$\mathbf{H}$	= the Jacobian
$\mathbf{s}$	= the state-vector (emissions)
$\mathbf{b}$	= the background concentration
$\boldsymbol{\varepsilon}_0$	= observation error



# The observations can be decomposed into constituent parts

$$z = Hs + b + \varepsilon_0$$

$$z = H_i s_i + b_{\text{INFLOW}} + b_{\text{EXP}} + \varepsilon_0$$

$H_i$  = the component of the Jacobian in the interior domain

$s_i$  = the emissions in the interior domain

$b_{\text{INFLOW}}$  = the boundary inflow variation

$b_{\text{EXP}}$  = the expected variation due to topography and albedo

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$$\mathbf{z} = \mathbf{H}_i\mathbf{s}_i + \mathbf{b}_{\text{INFLOW}} + \mathbf{b}_{\text{EXP}} + \boldsymbol{\varepsilon}_0$$

$$\mathbf{z} = \mathbf{H}_i\mathbf{s}_i + \mathbf{H}_0\mathbf{s}_0 + \mathbf{b}_{\text{APRIORI}} + \mathbf{A} * \mathbf{b}_{\text{CONST}} + \boldsymbol{\varepsilon}_0$$

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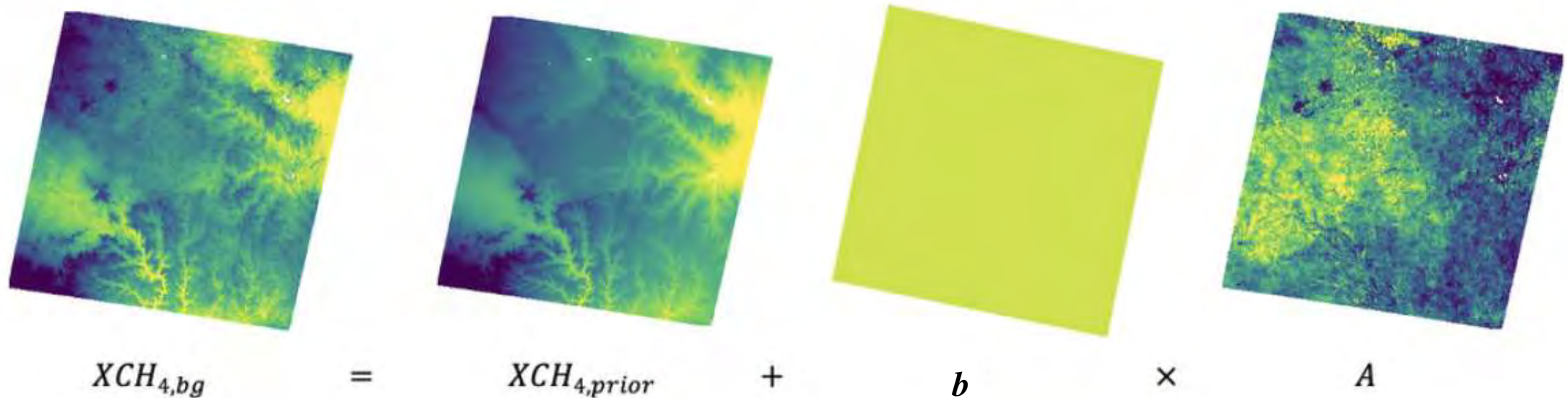
$\mathbf{b}_{\text{APRIORI}}$  = the apriori  $\text{XCH}_4$ , with variation only due to topography

$\mathbf{b}_{\text{CONST}}$  = the constant contribution to the background

# We construct a spatially resolved background to be subtracted from observations

4 main factors to consider in your background:

1. Topographic effect
2. Albedo effect
3. Latitudinal gradient
4. Averaging kernel effect



The diagram illustrates the construction of a spatially resolved background ( $XCH_4, bg$ ) as the sum of a prior ( $XCH_4, prior$ ) and a background ( $b$ ), multiplied by an averaging kernel ( $A$ ).

The equation is represented by four tilted rectangular plots arranged horizontally, separated by mathematical operators:

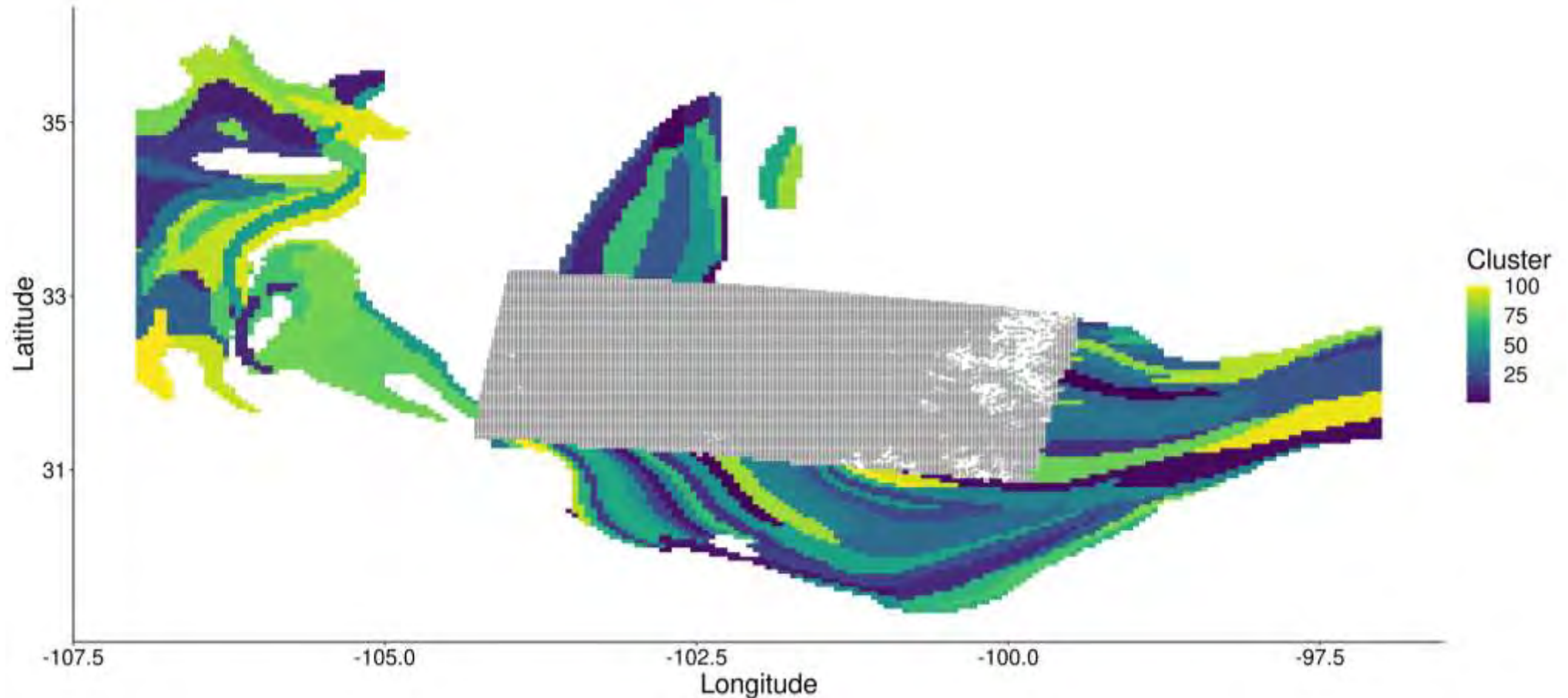
- The first plot, labeled  $XCH_4, bg$ , shows a spatial distribution with a mix of green, yellow, and dark blue.
- The second plot, labeled  $XCH_4, prior$ , shows a similar spatial distribution to the first.
- The third plot, labeled  $b$ , is a solid, uniform light green color.
- The fourth plot, labeled  $A$ , shows a spatial distribution with a mix of green, yellow, and dark blue, similar to the first and second plots.

The equation is represented as:

$$XCH_4, bg = XCH_4, prior + b \times A$$

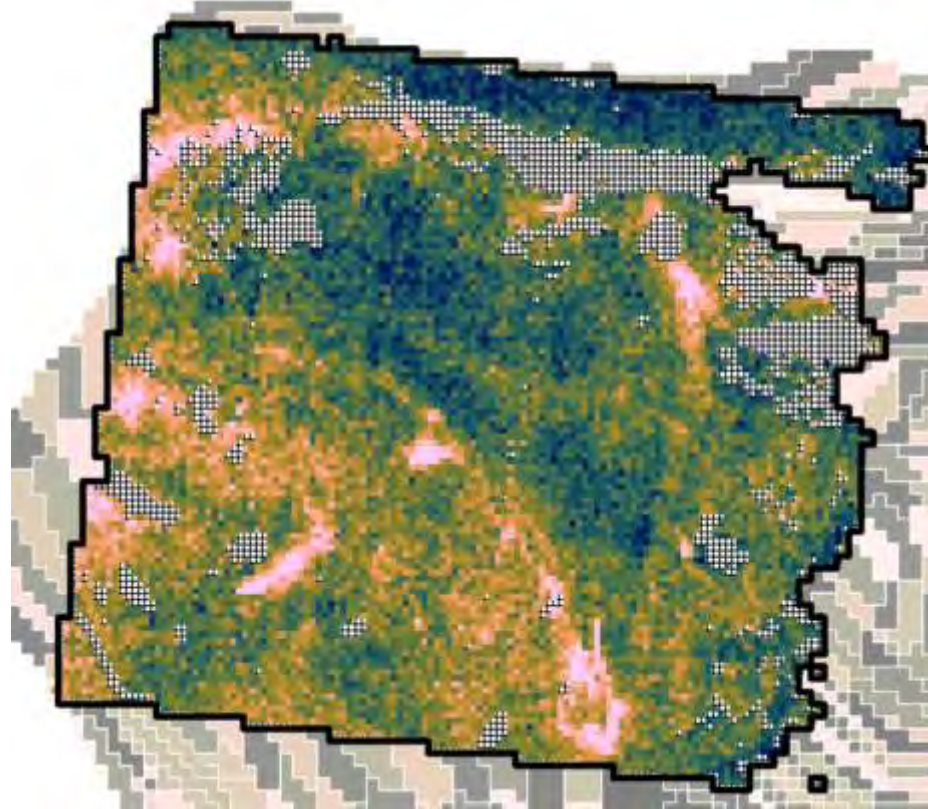


**We use KMEANS clustering of cosine distance to group emitters outside of the domain**

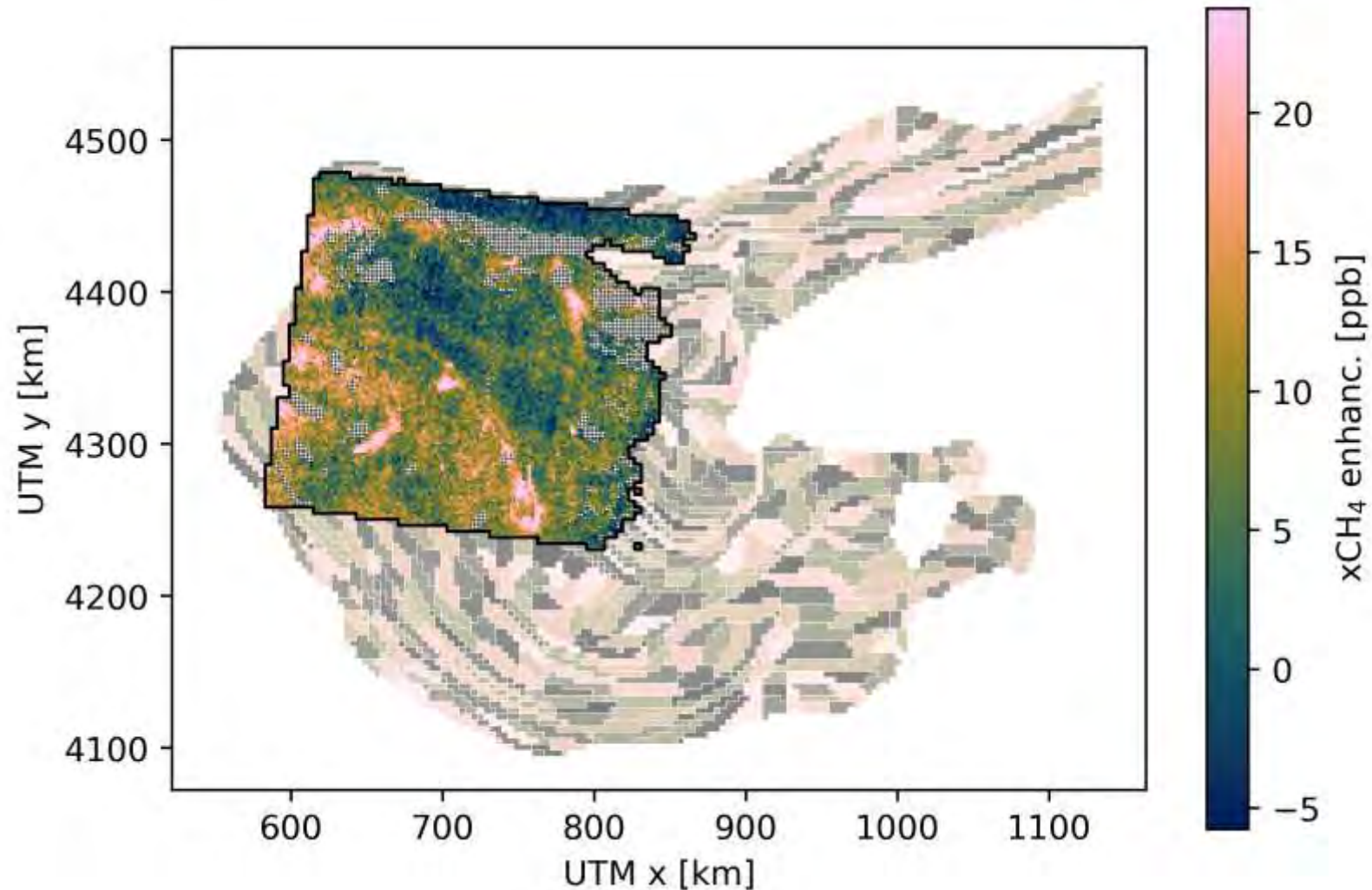


**$H_0$  = the component of the Jacobian in the exterior domain**  
 **$s_0$  = the emissions in the exterior domain**

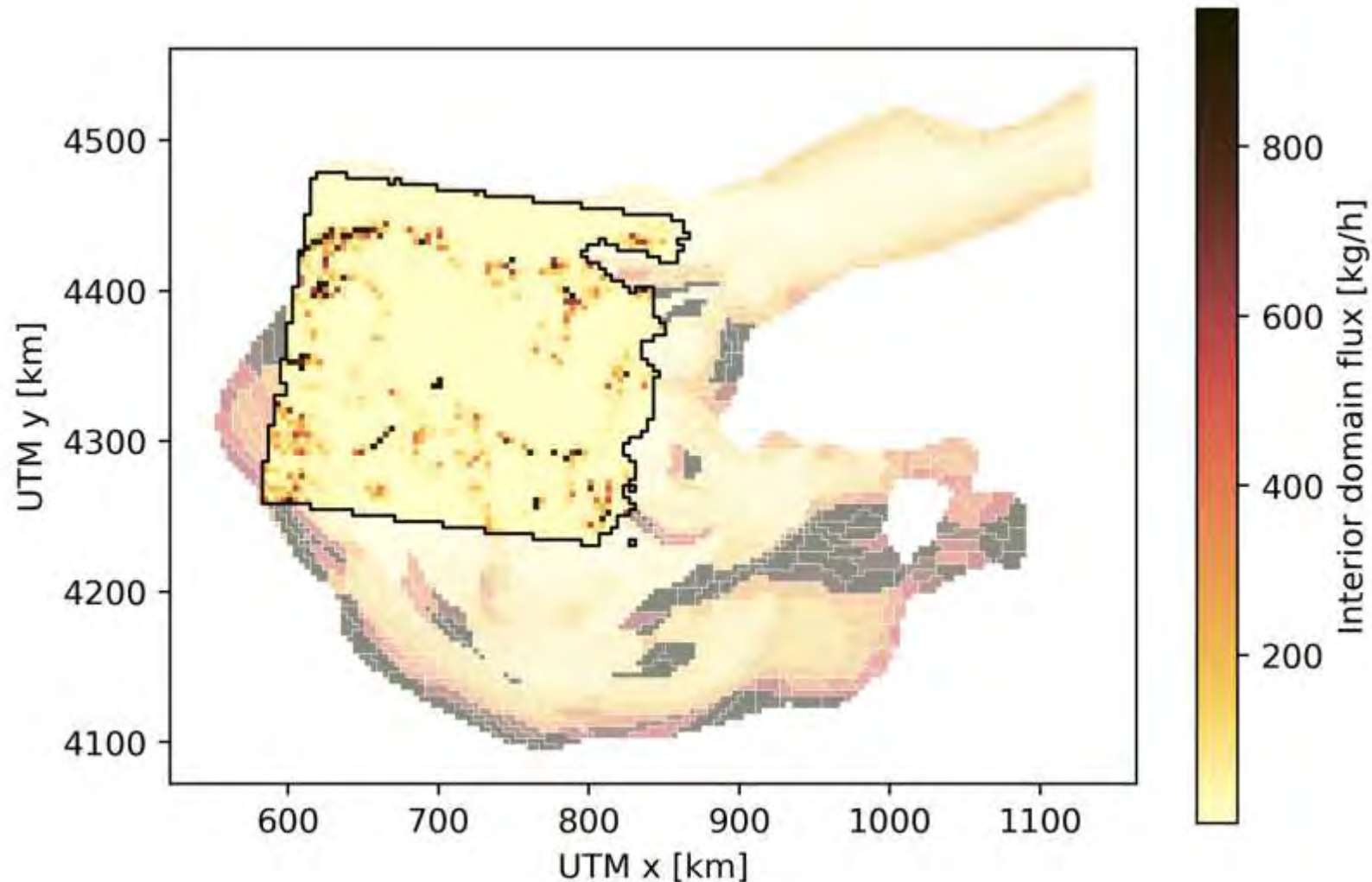
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with a diffuse lognormal prior to solve iteratively for emissions**



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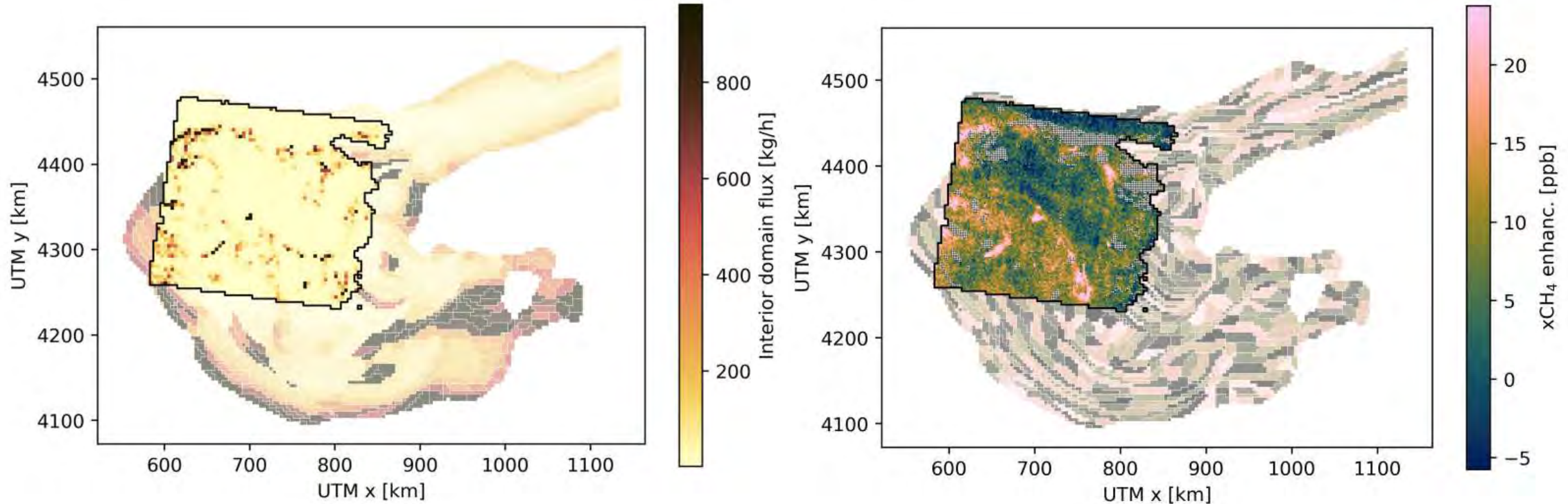


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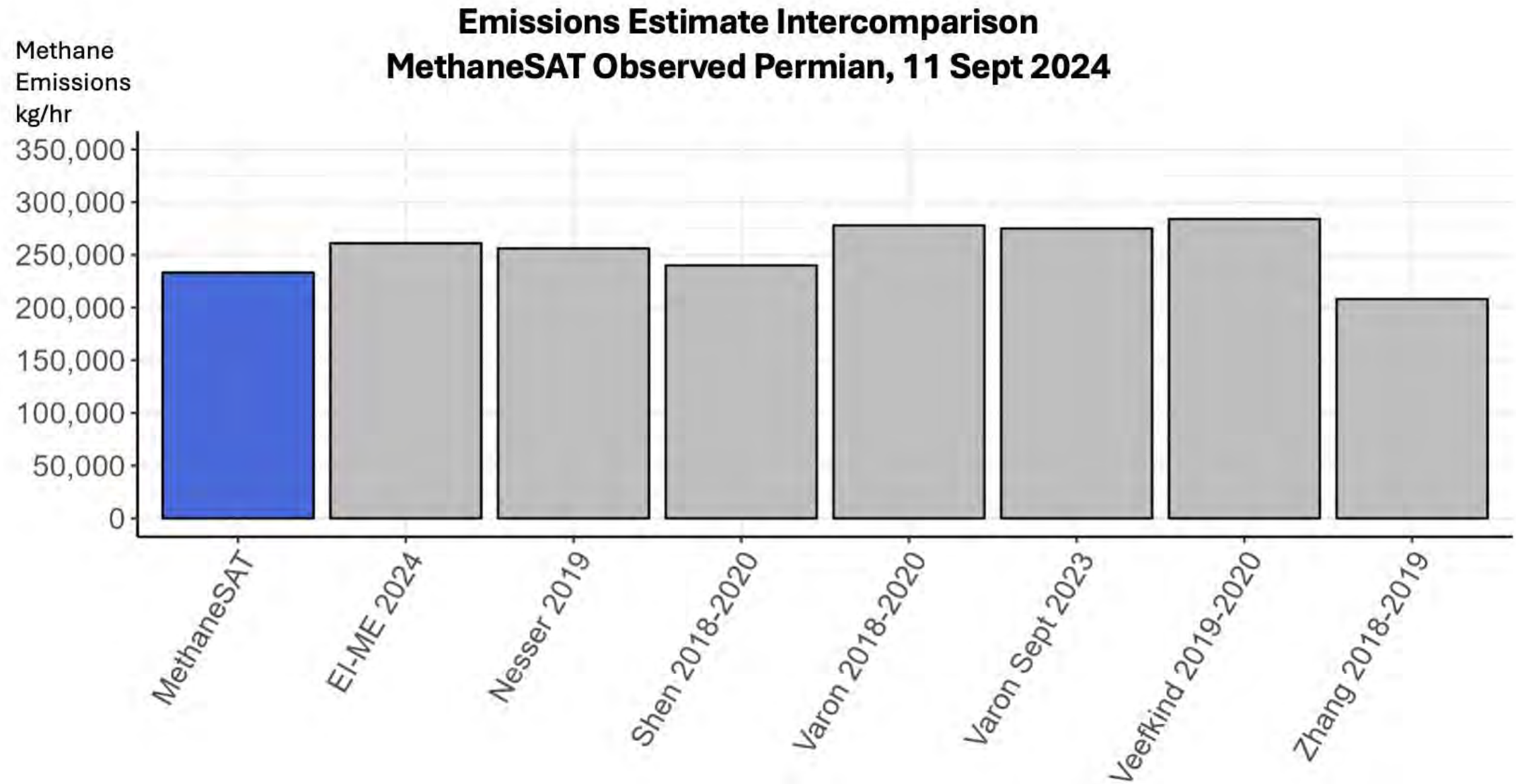




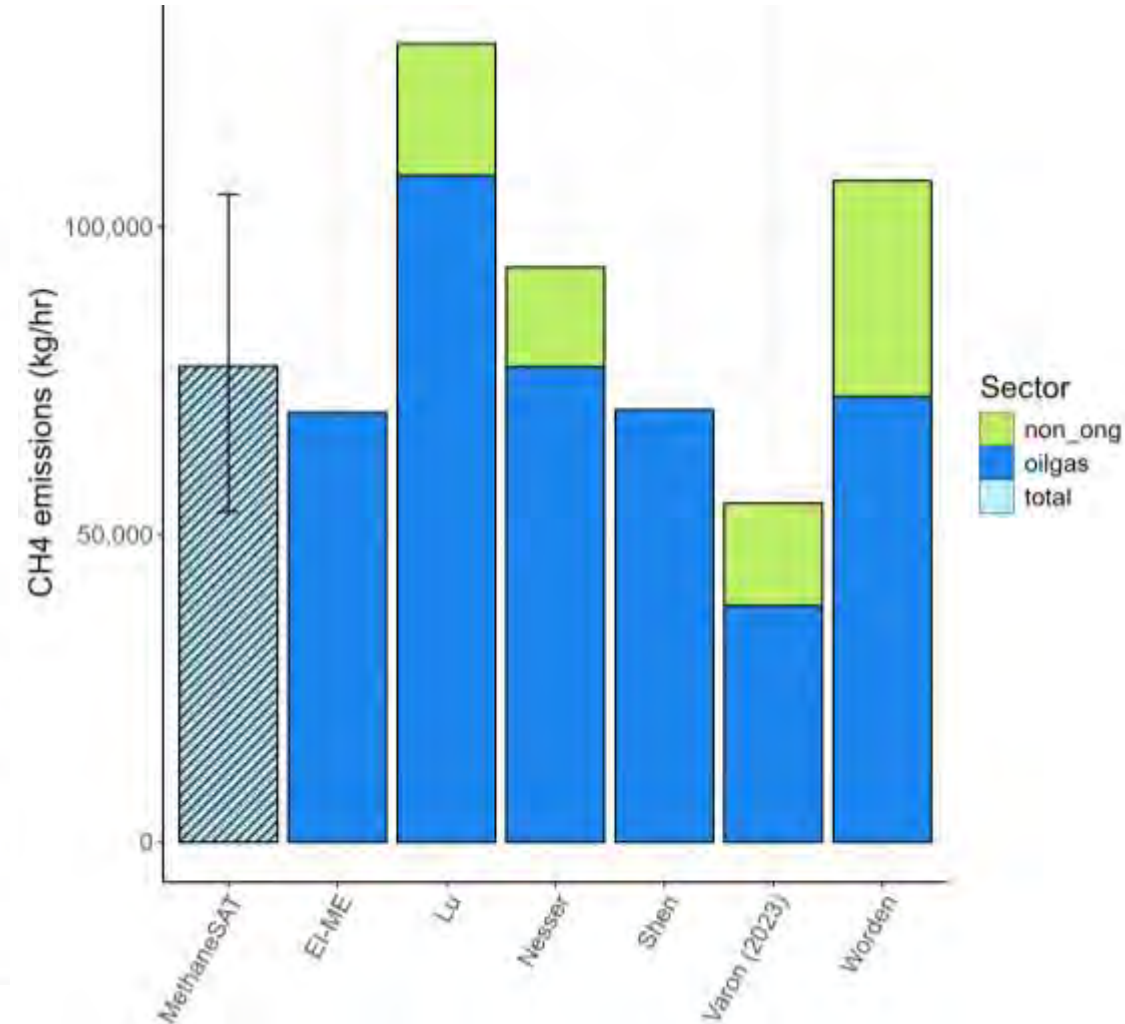
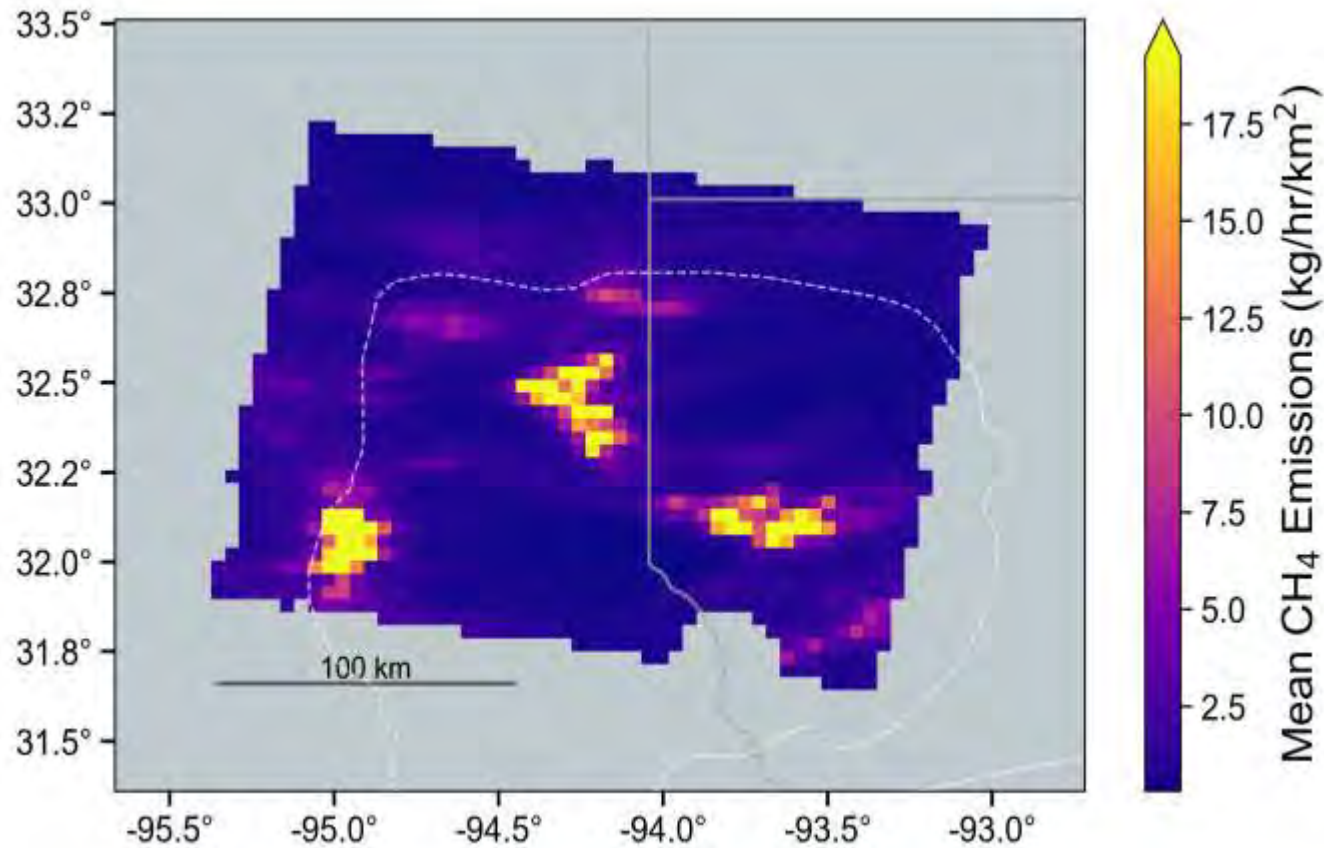
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# There is good agreement between MethaneSAT total emissions and other empirical data

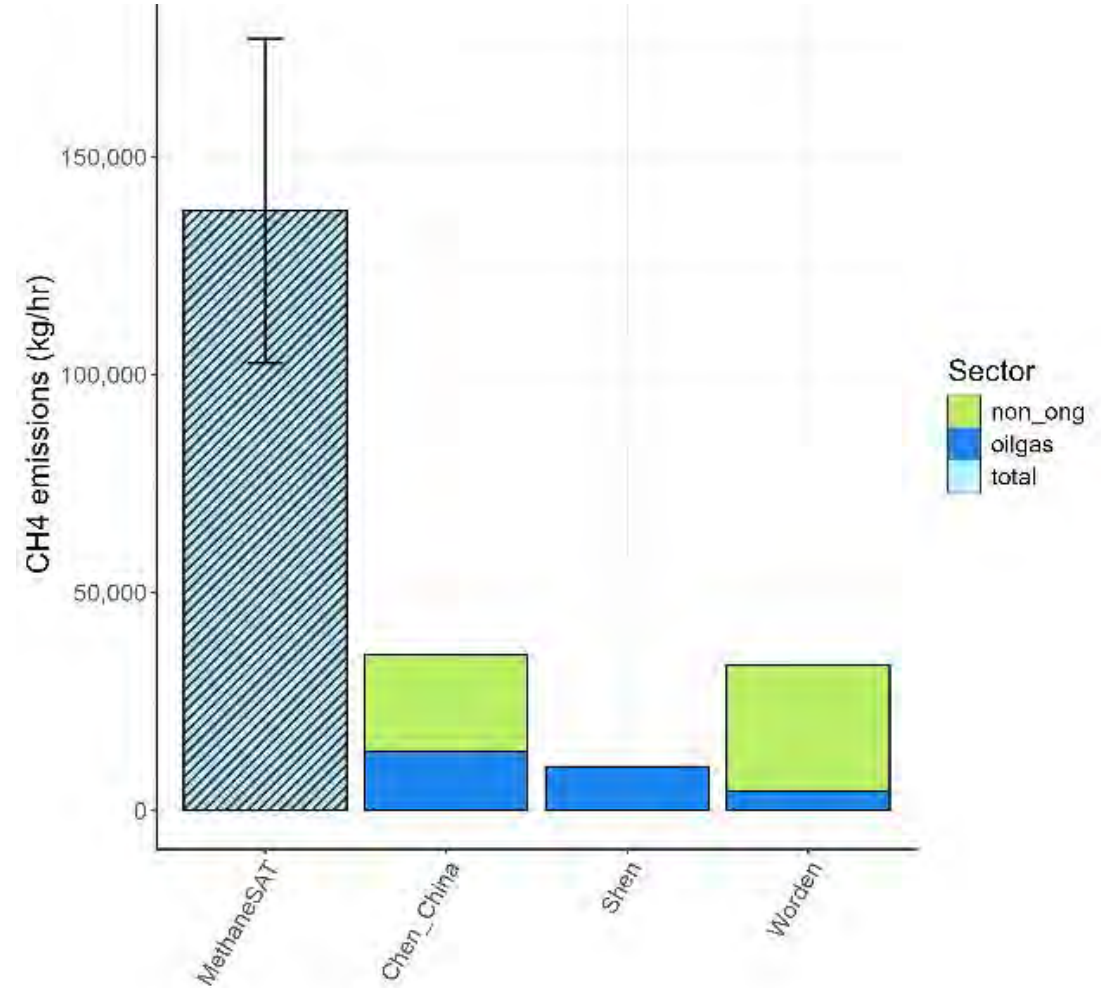
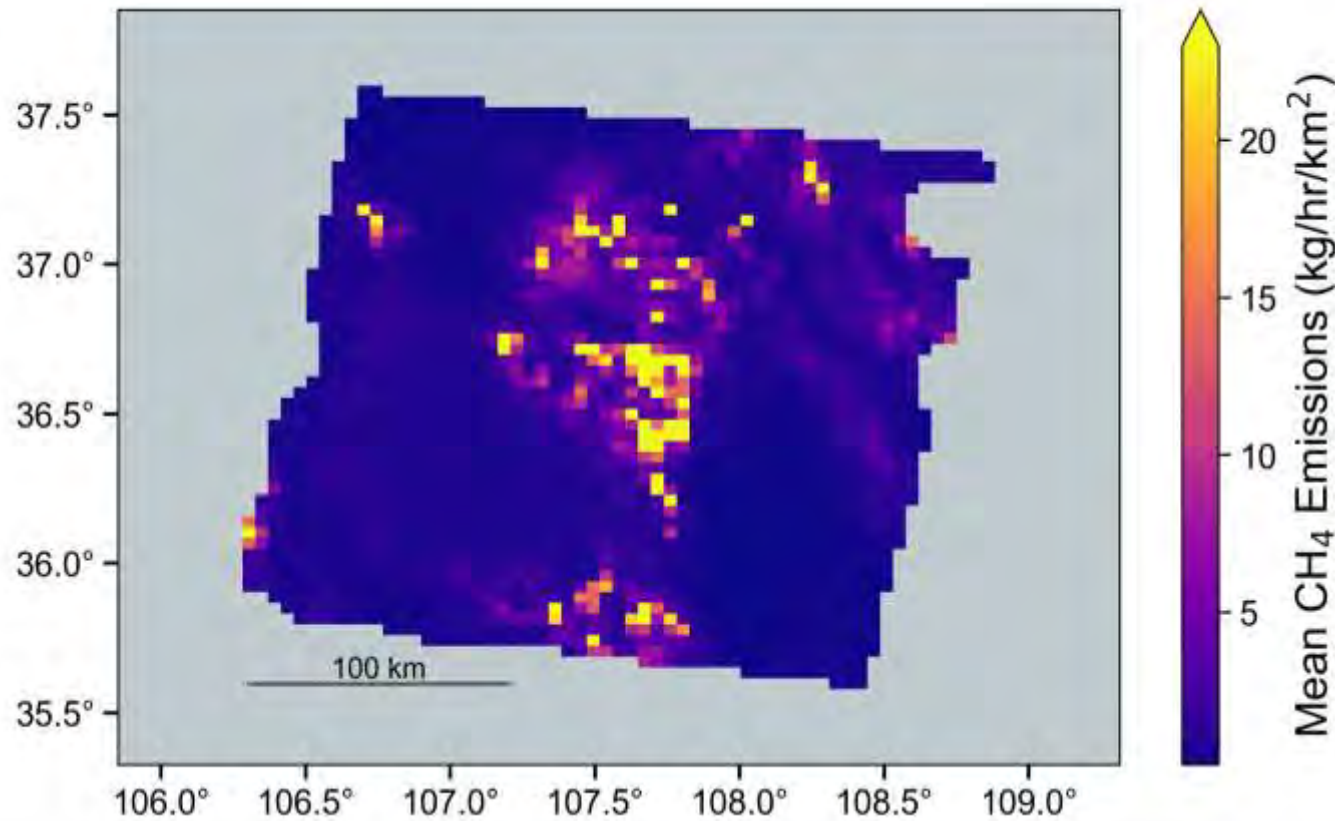


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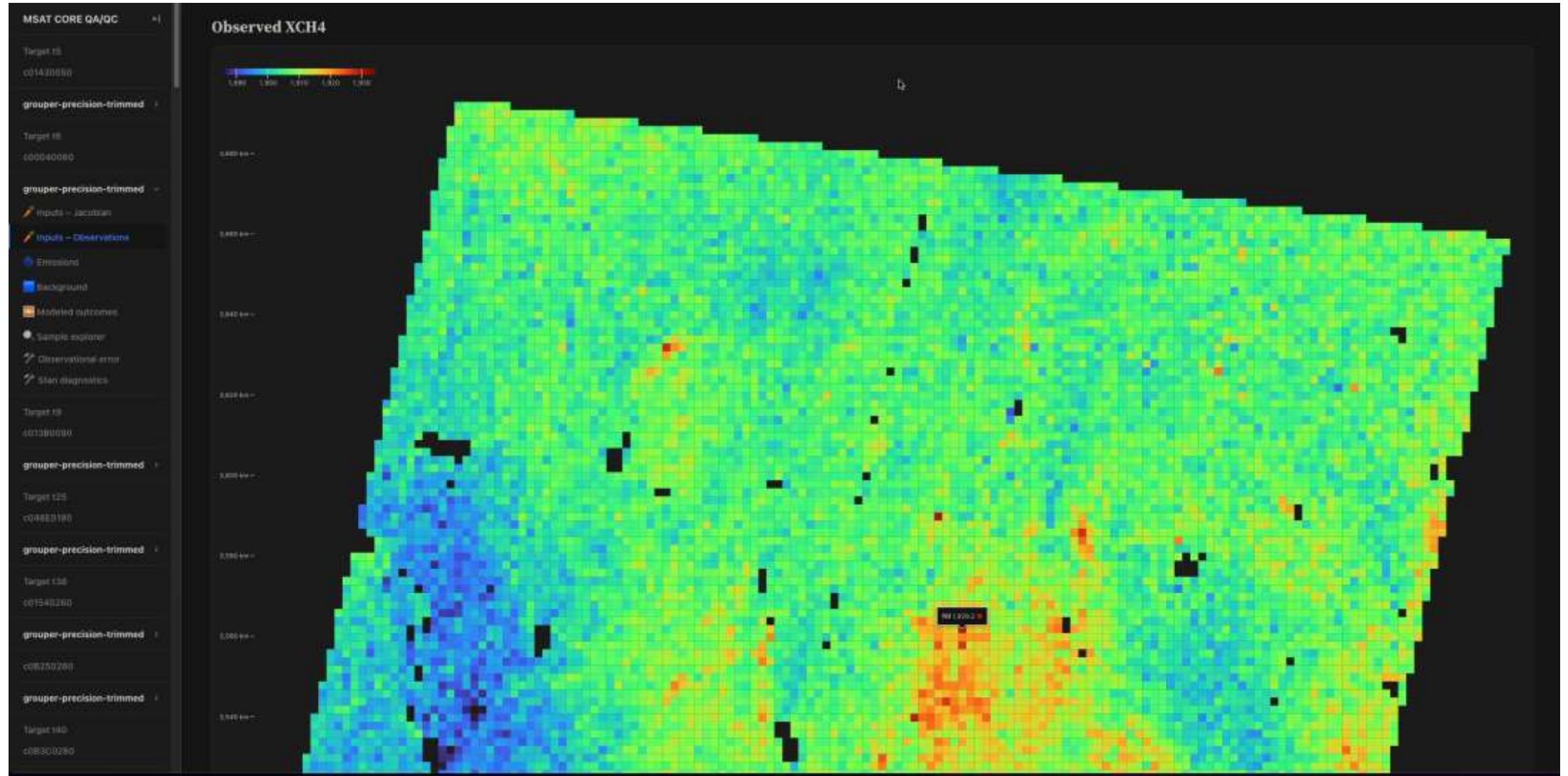


# Regional scale variations in emissions may be missed by national or global inversions

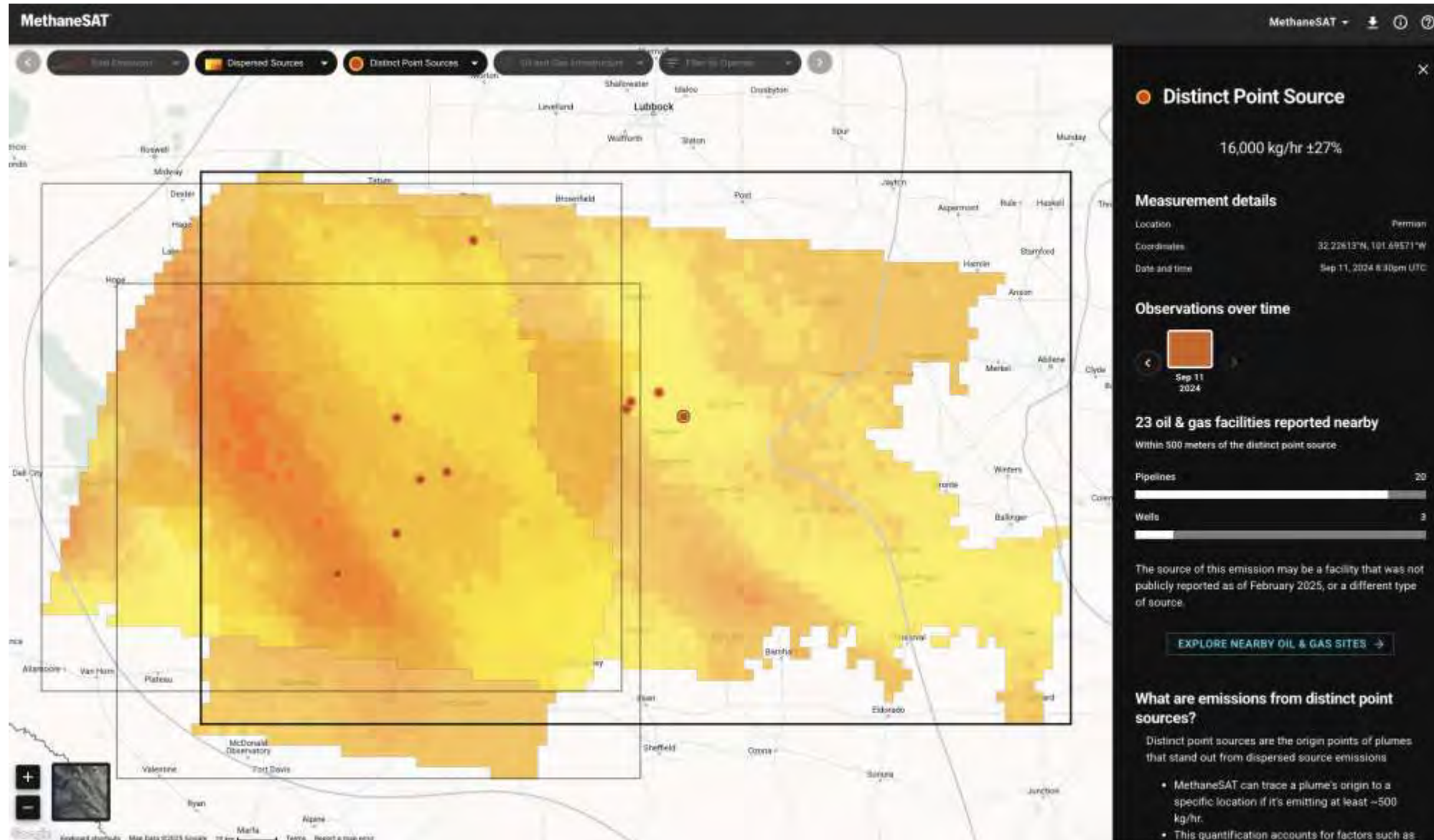




**Thanks to the work of our scientific programmers  
we are in the process of scaling up our inverse modeling capabilities**



# MethaneSAT enables comprehensive characterization of methane emissions from oil and gas basins



Data Portal:





# The success of MethaneSAT is thanks to numerous partners and collaborators

Steve Wofsy

Jonathan Franklin

Joshua Benmergui

Maryann Sargent

Maya Nasr

Ethan Kyzivat

Zhan Zhang

Apisada (Ju) Chulakadabba

Ethan Manninen

Eleanor Walker

Marvin Knapp

Ritesh Gautam

Mark Omara

Katlyn MacKay

Anthony Himmelberger

James Williams

Xiong Liu

Christopher Chan Miller

Kang Sun

Sebastien Roche

Javier Roger

Sara Mikaloff-Fletcher

Beata Bukosa

Alex Geddes

Harrison O'Sullivan Moffat

Kirstin Gerrand

Jasna Pittman

Bruce Daube

David Miller

Raia Ottenheimer

Marcus Russi

Sasha Ayvazov

Nick Lofaso

MethaneSAT Back End Software  
Engineering Team

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## Partners and Collaborators



## Data Portal:

