

# Non-local metrics applied to the comparison of CO<sub>2</sub> plumes and their sensitivities to mesoscale meteorology

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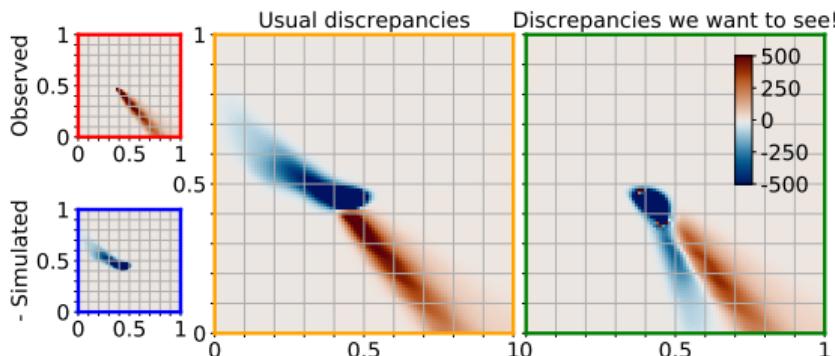


# Example: Case of a German power plant.

## ■ Experimental set-up:

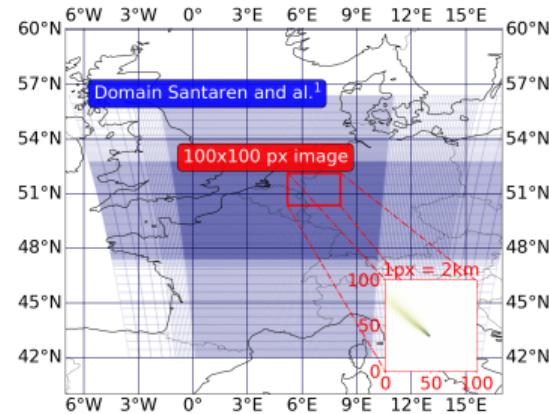
- Both images result from simulations.
- Same source location.
- Same emission rate.
- Same simulation period.
- Different meteorology.

## ■ Example:



## ■ Simulated CO<sub>2</sub> plumes:

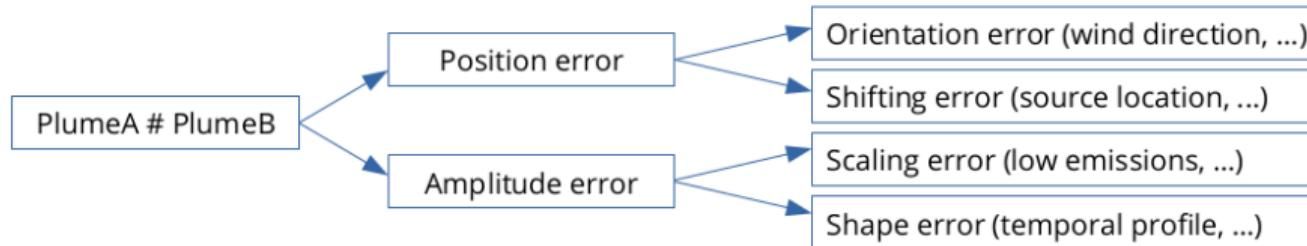
- No background concentrations.
- Images of 100x100 pixels.
- Resolution of 4 km<sup>2</sup>.
- Hourly output.



<sup>1</sup>: <https://doi.org/10.5194/amt-14-403-2021>

# Strategy

## ■ Matching errors decomposition:



## ■ Assumption:

- The position error is mainly driven by errors in the mesoscale wind field.

## ■ Aim for the new metrics:

- Avoid the double penalty issue (transform position error into amplitude error).
- Segregate the position error.

# New metrics

- **Baseline  $\mathcal{L}_2$  metric ( $d_{l2}$ ):**

- (+) Easy to compute.
- (-) double penalty issue.

- **New local metric ( $d_F$ ) freed from position error:**

- (+) Keep  $\mathcal{L}_2$  formalism while addressing double penalty issue.
- (-) Add a local minimisation process.

- **Non-local Wasserstein metric ( $w$ ):**

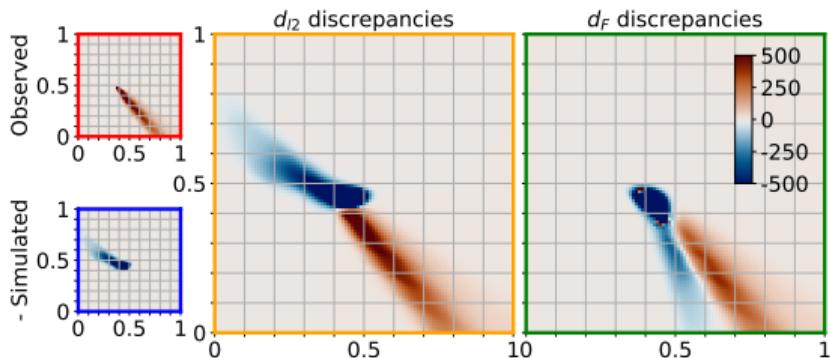
- (+) Separation of the errors sources.
- (-) Loose of the scale information.

- **Non-local Hellinger metric ( $w_F$ ):**

- (+) Cheap and freed of position error.
- (-) Ground on Gaussian puff assumption.

# Some results

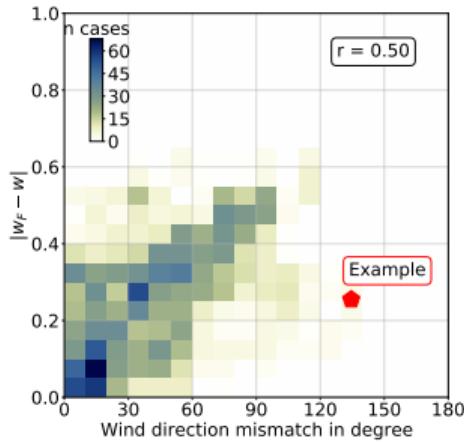
- Back to our example:



$d_{l2}$	$w$	$d_F$	$W_F$
388.6	0.3376	371.36	0.0830

Both  $d_F$  and  $w_F$  lead to lower values, and comparison with less position error.

- Results on ≈2000 different comparisons:



The shifting error is correlated to mesoscale wind direction changes.

# Discussions

## ■ What we learnt?

- To separate the position error from the amplitude error by using smarter metrics.
- The shifting error is mainly driven by mismatch in the wind direction.
- Remove the position error lead to a decrease in the sensitivity of the comparison with respect to changes in the wind field.
- The new metrics has to be tuned.
- Optimal transport metrics required the addition of a "mass" term to keep the scaling error.

## ■ To go further!

- The double penalty issue is addressed, but it creates an issue between orientation error and shape.
- Introduce these metrics in an assimilation process.
- Optimize the computation of Wasserstein distance.
- Get the sensitivities (Sobol index) according either meteorology or source profile.

## ■ Supplementary information: article will be submitted soon to AMT journal.